

MARKING SCHEME
SAMPLE PAPER
MATHEMATICS-CLASS XII

SECTION A			
Q.No.	Value Points	Marks	Total
1	36		1
2	$\begin{bmatrix} 6 & -1 \\ -7 & 3 \end{bmatrix}$		1
3	$(\sqrt[3]{x-3})$		1
4	$\frac{2\pi}{5}$		1
5	4x-4y+33=0		1
6	$\sqrt{5}$		1
7	2		1
8	$\frac{3}{2\sqrt{2}} \tan^{-1}(\sqrt{2} x^2) + c$		1
9	X=4 and y=3		1
10	$\frac{-9}{\sqrt{14}}$		1
SECTION B			
11	Property of Id element Id element (1,0) Prtoperty of Inverse Inverse doesn't	1 1 1 1	4
12	Application of correct formula Correct equation Solving $4x^2 - 31x - 8 = 0$ and $x=8$ OR Application of formula Second application Combining to get $\tan^{-1}\frac{25}{25} = \frac{\pi}{4}$	1 1 2 1 1 2	4
13	Use of three properties and Conclusion	2 2	4
14	Calculation of LHL Calculation of RHL Conclusion LHL=RHL=f(0)=3/2	11/2 11/2 1	4

15	Finding of dy/dx and rearranging OR Writing correct derivatives Rearrangement and proof	2+2 1+1 2	4
16	Finding first derivative Simplification Expressing as perfect squares and conclusion	1 1 2	4
17	Expressing the denominator in cos or sin. Applying the correct integral Simplification.or any other alternate methods OR Using partial fraction and finding three constants Evaluating three integrals and simplification, An: $\frac{11}{10}\log\left(\frac{\sqrt{x^2+1}}{x+3}\right) - \frac{3}{11}\tan^{-1}x + c$	1 1 2 2 2	4
18	Identification and I.F-linear and I.F.is $\text{Cosec}^3 x$ Solving : $y\text{Cosec}^3 x = \int \text{Sin}2x \text{Cosec}^3 x dx + c$ Writing particular solution: $y = \sin^2 x(-2 + 4\sin x)$ OR Separating the variables Integrating by substitution Solving and writing Particular solution: $\frac{(1+\log x)^2}{2} + \tan^{-1}y = \frac{\pi}{4} + \frac{1}{2}$	11/2 2 1/2 1 1 2	4
19	Identification and substitution Separating variables Integrating and replacing v by x/y Solu. Is $x + ye^{\frac{y}{x}} = c$	1 1 2	4
20	Concept of unit vector Sum of $2\hat{i} + 4\hat{j} - 5\hat{k}$ and $\lambda \hat{i} + 2\hat{j} + 3\hat{k}$ Modulus of the above sum Dot product and value of $\lambda=1$	1/2 1 1/2 2	4
21	Equation of line is $\frac{x-1}{a} = \frac{y-2}{b} = \frac{z-3}{c}$ Concept of normal and line(perpendicular) Solving of equations $a-b+2c=0$ and $3a+b+c=0$ as $a=-3, b=5$ and $c=4$ Writing the final equation	1 1 11/2 1/2	4
22	Probabilities for not solving Required probability = $P(\bar{A} \bar{B} C) + P(\bar{A} B \bar{C}) + P(A \bar{B} \bar{C}) = \frac{11}{24}$	11/2 21/2	4
SECTION C			
23	$\det A = -1 \neq 0, A^{-1}$ exists	1	

	$\text{adj}A = \begin{bmatrix} 0 & 1 & 2 \\ -2 & -9 & -23 \\ 1 & 5 & 13 \end{bmatrix} \& B = \begin{bmatrix} 11 \\ 5 \\ -3 \end{bmatrix}$ $X = \frac{1}{ A } (\text{adj}A) B \text{ gives } x=1, y=2 \text{ and } z=3$	3 2	6
24	<p>Writing the correct relation in one variable Step wise application of differentiation Obtaining the correct relation and max. volume = $\frac{8}{9}\pi R^3(3 - \sqrt{3})$</p> <p>OR</p> <p>Finding the correct relation in one variable Step wise application of differentiation Obtaining the correct relation</p>	2 2 2 2 2 2	6
25	<p>Giving substitution as $x = a \tan^2 \theta$ and simplification <i>Replacing dx by $2a \sec^2 \theta \tan \theta$ and applying integration by parts</i> Application of limits and simplification, An: $\frac{a}{2}(\pi - 2)$</p> <p>OR</p> <p>Application of property and 21 Evaluating integral by substitution Applying limits and simplification. An : $\frac{\pi^2}{4}$</p>	2 2 2 1+1 2 2	6
26	<p>Identification of the given curves and rough sketch Solving the equations and finding limit of integrals $4x^2 + 16x - 9 = 0$ gives $x = 1/2$ and</p> $\text{Area} = 2 \int_0^{1/2} 2\sqrt{x} dx + 2 \int_{1/2}^3 \sqrt{\frac{9}{4} - x^2} dx = \frac{9\pi}{8} + \frac{\sqrt{2}}{6} - \frac{9}{4} \sin^{-1} \left(\frac{1}{3} \right)$	1 2 3	6
27	<p>Equation of plane passing through (-1,2,1) is $A(x+1)+B(y-2)+C(z-1)=0$ Equation of a line joining (-3,1,2) and (2,3,4) is $\frac{x+3}{5} = \frac{y-1}{2} = \frac{z-2}{2}$ Since the plane is perpendicular to the line, line and normal are parallel and $A=5, B=2$ and $C=2$ Equation of plane is $5x+2y+2z-1=0$ Distance from origin to the plane is $\frac{1}{\sqrt{13}}$ units</p>	1 2 1 1 1	6
28	<p>Let the old man travel x km at 25km/hr and y km at 40km/hr Objective function is $z=x+y$ Constraints : $x \geq 0, y \geq 0$ $2x+5y \leq 100$ and $\frac{x}{25} + \frac{y}{40} \leq 1$ ie, $8x + 5y \leq 200$ Graphing two lines with scale and shading of common region Locating the corner points as $O(0,0), (25,0), \left(\frac{50}{3}, \frac{40}{3}\right)$ and $(0,20)$ and calculation of $z(\text{max})=30$ at $\left(\frac{50}{3}, \frac{40}{3}\right)$</p>	$\frac{1}{2}$ $\frac{1}{2}$ 2 2 1	6
29	<p>Let E_1 be the event of selecting a bag from the first group And E_2 be the event of selecting a bag from the second group</p> <p>A be the event of ball drawn is white</p>	11/2	

	<p>Then, $P(E1)=3/5, P(E2)=2/5$ and $P(A/E1)=5/8, P(A/E2)=5/8$</p> <p>Therefore the required probability, $P(E1/A) = \frac{P(E1)P(\frac{A}{E1})}{P(E1)P(\frac{A}{E1}) + P(E2)P(\frac{A}{E2})}$</p> $= \frac{\frac{3}{5} \times \frac{5}{8}}{\frac{3}{5} \times \frac{5}{8} + \frac{2}{5} \times \frac{1}{3}} = \frac{45}{61}$	<p>2 1</p> <p>11/2</p>	<p>6</p>
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